

## TRUE AND FALSE QUESTIONS.

Question - State whether the following statements are True or False —

- ① The system of linear equations  $x - y = 1$   
&  $2x - 2y = 3$  has a unique solu.
- ② If  $A$  &  $B$  are matrices of same size, then  $AB = BA$ .
- ③ If  $A$  is  $3 \times 4$  and  $B$  is  $4 \times 2$  matrix, then  $(AB)^T$  is matrix of size  $2 \times 3$ .
- ④ The matrix  $\begin{bmatrix} 1 & 2 \\ 1 & 2 \end{bmatrix}$  is not Invertible.
- ⑤ The matrix  $\begin{bmatrix} -5 & 3 \\ 2 & -1 \end{bmatrix}$  is the inverted coefficient matrix of the system of equations —  
 $x + 3y = 4$   
 $2x + 5y = 7$
- ⑥ A diagonal matrix is both upper and lower triangular matrix at same time.

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⑦ The determinant of the matrix  $A = \begin{bmatrix} 1 & 1 & 0 \\ 2 & 4 & 1 \\ 3 & 3 & 0 \end{bmatrix}$  is 2.

⑧ The absolute values of minors and cofactors of the elements of a square matrix are identical.

⑨ If matrix  $A$  is invertible, then  $A^T$  is also invertible.

⑩ If  $A$  is a square matrix with two proportional rows, then  $\det(A) = 0$ .

⑪ If  $A$  is a square matrix, then  $\det(A^{-1}) = \frac{1}{\det(A)}$ .

⑫ If  $A$  &  $B$  are square matrices of same size, then  $\det(AB) \neq \det(A) \cdot \det(B)$

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⑬ If  $(2, -1)$  and  $(3, 1)$  are the initial and terminal points of a vector, then  $(1, -2)$  is the component of the vector.

⑭ The vectors  $(1, 2, 3)$  and  $(-3, 2, 1)$  have same magnitude.

⑮ The vectors  $(4, 10, 0)$  and  $(-5, 2, 9)$  are orthogonal to each other.

⑯ If  $u = (1, 3, -2, 7)$  and  $v = (0, 7, 2, 2)$ , then distance between  $u$  &  $v$  is  $\sqrt{58}$ .

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- (17) The set  $\mathbb{R}^3$  is a subspace of  $\mathbb{R}^4$ .
- (18) Any plane passing through the Origin is a subspace of  $\mathbb{R}^3$ .
- (19) The set  $\{(1,0,0), (0,1,0), (0,0,1)\}$  of vectors in  $\mathbb{R}^3$  is Linearly Independent.
- (20) If a set has exactly one <sup>non-zero</sup> vector, then this set must be Linearly Dependent.
- (21) All linearly independent set in a subspace  $W$  is a basis for  $W$ .
- (22) The basis of a vector space is not unique.
- (23) If 'A' is a  $3 \times 3$  matrix such that  $|A| \neq 0$ , then row vectors of 'A' span  $\mathbb{R}^3$ .
- (24) If 'A' is  $m \times n$  matrix, then row space of 'A' and column space of 'A' have different dimension.

- (25) The Sum of eigenvalues of a square matrix is same as its Trace.
- (26) The eigenvalues of the matrix  $A = \begin{bmatrix} 2 & 0 & 0 \\ 6 & -1 & 0 \\ 7 & 2 & 4 \end{bmatrix}$  are 2, 4 and 0.
- (27) The Product of eigenvalues of a square matrix is same as its Determinant.
- (28)  $(1, 0, 2)$  is the real part of the complex vector  $(i+1, ai, 2i+2)$ .
- (29) The characteristic polynomial of  $2 \times 2$  matrix 'A' is of degree 3.
- (30) A square matrix 'A' is invertible iff  $\lambda = 0$  is an eigenvalue of 'A'.
- (31) If a matrix 'A' of size  $n \times n$  has  $n$  linearly independent eigenvectors then matrix 'A' is not Diagonalizable.
- (32) If an  $n \times n$  matrix 'A' has  $n$  eigenvalues, then 'A' is Diagonalizable.
- (33) If 'A' is real symmetric matrix, then 'A' has complex eigenvalues.

- (34) The inner product of two vectors cannot be a negative real no.
- (35) The inner product of a vector with itself can be negative real no.
- (36) If  $u$  &  $v$  are orthogonal vectors in an inner product space, then  $\langle u, v \rangle \neq 0$ .
- (37) If  $u$  &  $v$  are unit orthogonal vectors in an inner product space, then  $\|u+v\| = 2$ .
- (38) If  $u = (3, 4)$  is a vector in  $\mathbb{R}^2$ , then the length of  $u$  is 7.



- (39) A square matrix 'A' is Orthogonal, if  $\bar{A}^{-1} = A$ .
- (40) A square matrix 'A' is Unitary, if  $A^* = A$ .
- (41) The inverse of an Orthogonal matrix is not necessarily Orthogonal.
- (42) If determinant of a matrix is 1 or -1, then the matrix is Orthogonal.
- (43) If a matrix 'A' is Orthogonal, then  $\det(A) = 1$  or  $-1$ .
- (44) Every symmetric matrix is Orthogonally Diagonalizable.
- (45) In case of real matrices, Unitary and Orthogonal matrices are same.
- (46) The eigenvalues of a Hermitian matrix are all real.

- (47) If  $T: V \rightarrow V$  is an operator such that  $T(v) = 2v, \forall v \in V$ , then  $T$  is Linear.
- (48) If  $T: V \rightarrow W$  is an isomorphism, then kernel of  $T$  is the zero subspace.
- (49) The function  $T: \mathbb{R}^2 \rightarrow \mathbb{R}^3$  given by  $T(x_1, x_2) = (2x_1 + 3x_2, 4x_2 - 1 - x_1, x_1)$  is Linear.
- (50) If  $T$  is translation operator, then it is Linear.

- (51) Every square matrix need not have LU-decomposition.
- (52) The dominant eigenvalue is 5 for set of eigenvalues  $\{3, 4, 5, -5\}$ .
- (53) If 'A' is an  $m \times n$  matrix, then  $A^T A$  is an  $n \times n$  matrix.
- (54) If 'A' is an  $m \times n$  matrix, then  $A^T A$  is Orthogonally diagonalizable.
- (55) In Linear Programming Problems, all variables are restricted to positive values only.
- (56) In LPP, a linear objective function is to be optimized.
- (57) One of the quickest way to plot a constraint is to find the two points where the constraint crosses the axes and draw a straight line between these points.
- (58) The graphical method is used only when LPP have exactly two unknown variables.

### ANSWERS

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|--------|--------|--------|--------|--------|--------|
| (1) F  | (11) T | (21) F | (31) F | (41) F | (51) T |
| (2) F  | (12) F | (22) T | (32) F | (42) F | (52) F |
| (3) T  | (13) F | (23) T | (33) F | (43) T | (53) T |
| (4) T  | (14) T | (24) F | (34) F | (44) T | (54) T |
| (5) T  | (15) T | (25) T | (35) T | (45) T | (55) F |
| (6) T  | (16) T | (26) T | (36) F | (46) T | (56) T |
| (7) F  | (17) F | (27) T | (37) F | (47) F | (57) T |
| (8) T  | (18) T | (28) T | (38) F | (48) T | (58) T |
| (9) T  | (19) T | (29) F | (39) T | (49) F |        |
| (10) T | (20) F | (30) F | (40) F | (50) T |        |

## OBJECTIVE TYPE QUESTIONS

Question - Select one of alternatives from the following questions as your answer —

① Which of the following is Reduced Row Echelon form —

- (a)  $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$  (b)  $\begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  (c)  $\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 3 \end{bmatrix}$  (d) None

② The inverse of the matrix  $\begin{bmatrix} -2 & 3 \\ -1 & 1 \end{bmatrix}$  is —

- (a)  $\begin{bmatrix} 1 & -3 \\ 1 & -2 \end{bmatrix}$  (b)  $\begin{bmatrix} 1 & 3 \\ -1 & -2 \end{bmatrix}$  (c)  $\begin{bmatrix} -1 & 3 \\ -1 & 2 \end{bmatrix}$  (d)  $\begin{bmatrix} 1 & 3 \\ -1 & -2 \end{bmatrix}$

③ If  $A = \begin{bmatrix} 2 & -1 & 5 \\ 3 & 4 & 2 \end{bmatrix}$ , then  $((A^T)^T)^T$  is —

- (a)  $\begin{bmatrix} 2 & -1 & 5 \\ 3 & 4 & 2 \end{bmatrix}$  (b)  $\begin{bmatrix} 2 & 3 \\ -1 & 4 \\ 5 & 2 \end{bmatrix}$  (c)  $(A^3)^T$  (d) does not exist.

④ The inverse of an <sup>invertible</sup> Upper triangular matrix is —

- (a) Upper triangular (b) lower triangular (c) diagonal (d) does not exist.

⑤ If  $A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$ , then matrix A is —

- (a) Upper triangular (b) lower triangular (c) diagonal (d) all of the above.

⑥ If  $A = \begin{bmatrix} 3 & 2 & -1 \\ -1 & 8 & 7 \\ 4 & -3 & 1 \end{bmatrix}$ , then the values of minor and cofactor corresponding to the entry  $a_{23}$  are — (a) 1, -1 (b) -1, 1 (c) -17, 17 (d) 17, -17

⑦ If the determinant of  $A = \frac{1}{2}$ , then  $\det(A^{-1})$  is —

- (a)  $\frac{1}{2}$  (b) 2 (c)  $-\frac{1}{2}$  (d) None

⑧ If  $A = \begin{bmatrix} 2 & -1 \\ 5 & -2 \end{bmatrix}$ , then adjoint of A is —

- (a)  $\begin{bmatrix} -2 & 1 \\ -5 & 2 \end{bmatrix}$  (b)  $\begin{bmatrix} -2 & 5 \\ 1 & 2 \end{bmatrix}$  (c)  $\begin{bmatrix} -2 & -1 \\ -5 & 2 \end{bmatrix}$  (d)  $\begin{bmatrix} 2 & -1 \\ -5 & -2 \end{bmatrix}$

⑨ If  $u = (2, 1, 3)$  and  $v = (-1, 3, 2)$ , then the distance between u & v is —  
(a)  $\sqrt{13}$  (b)  $\sqrt{14}$  (c)  $\sqrt{15}$  (d)  $\sqrt{17}$ .

⑩ If  $\|u\| = 1$ ,  $\|v\| = 2$ ,  $u \cdot v = 0$ , then the angle between u & v is —  
(a) 0 (b)  $\pi$  (c)  $\frac{\pi}{2}$  (d)  $\frac{\pi}{3}$ .

⑪ If  $\theta$  is the angle between  $u = (1, 2, 3)$  &  $v = (3, 2, 1)$  then  $\cos \theta$  is —

- (a)  $\frac{10}{\sqrt{14} \sqrt{14}}$  (b)  $\frac{5}{7}$  (c) both (a) & (b) (d) Neither (a) nor (b)

⑫ The vector  $(2, 0, 1, -1)$  is orthogonal to the vector —

- (a)  $(0, 1, 2, -1)$  (b)  $(0, 2, -1, 1)$  (c)  $(1, -1, 0, 2)$  (d)  $(0, -1, 2, 1)$

⑬ If  $u = (2, -3, 1)$  and  $v = (0, 5, 7)$  are two vectors in  $R^3$ , then  $u \times v$  is —

- (a)  $(-26, 14, 10)$  (b)  $(-26, -14, 10)$  (c)  $(-26, -14, -10)$  (d)  $(26, 14, 10)$



- (14) Which of the following set of vectors in  $\mathbb{R}^3$  is a basis —  
 (a)  $\{(1, 2, -4), (-8, 14, 6), (3, 4, -9), (1, 0, 0)\}$  (b)  $\{(1, 2, 5), (2, 5, 1), (1, 5, 2)\}$   
 (c)  $\{(1, 2, 3), (0, 0, 0), (3, 2, 1)\}$  (d)  $\{(3, 2, -4), (24, 16, -32)\}$
- (15) The dimension of the vector space of  $4 \times 3$  matrices of real numbers under the usual addition and scalar multiplication of matrices is —  
 (a) 7 (b) 12 (c) 6 (d) Infinite
- (16) For which value of  $a$  and  $b$  the vector  $W = (1, -3, 4)$  is a linear combination of  $u = (2, 4, 0)$  and  $v = (1, 4, -2)$   
 (a)  $a=1, b=-2$  (b)  $a=-3, b=-2$  (c)  $a=-1, b=-2$  (d) None
- (17) If 'A' is a  $4 \times 5$  matrix with rank 3, then nullity of 'A' is —  
 (a) 1 (b) 2 (c) 3 (d) 0
- (18) If the rank of a  $4 \times 4$  matrix is equal to 3, then —  
 (a) the matrix is invertible (b) the dimension of null space is 4.  
 (c) the dimension of null space is 3 (d) the dimension of row space is 3.
- (19) Let  $S = \{v_1, v_2, v_3\}$  is a basis of  $V$  and  $v = 2v_1 - 3v_2$ . Then the coordinate vector of  $v$  relative to  $S$  is —  
 (a)  $(2, 3, 0)$  (b)  $(2, 0, -3)$  (c)  $(2, -3, 0)$  (d)  $(2, -3)$ .

- (20) The eigenvalues of a matrix,  $A = \begin{bmatrix} 1 & 0 & 0 \\ 2 & 2 & 0 \\ 0 & 3 & -1 \end{bmatrix}$  are —  
 (a)  $\{1, 2, 3\}$  (b)  $\{1, 2, 2\}$  (c)  $\{1, 2, 0\}$  (d)  $\{1, -1, 2\}$
- (21) If  $\{1, 2, 3\}$  are the eigenvalues of a matrix, then its Trace & Determinant are —  
 (a) 3, 3 (b) 4, 4 (c) 6, 6 (d) 5, 5
- (22) If '0' is an eigenvalue of a square matrix 'A', then A is —  
 (a) invertible (b) not invertible (c) an identity matrix (d) None
- (23) The eigenvalues of a real symmetric matrix are —  
 (a) complex only (b) complex and real both (c) always real (d) always zero.
- (24) If ' $\lambda$ ' is an eigenvalue of  $n \times n$  matrix A, then system of eqn.  $(\lambda I - A)x = 0$  has —  
 (a) trivial solu. only (b) non-trivial solutions (c) both trivial & non-trivial (d) None  
 Solu

- (25) If  $u = (1, -2, 3)$ ,  $v = (2, 0, 1)$  and  $k=1$ , then the value of  $\langle ku, v \rangle$  is —  
 (a) 10 (b) -10 (c) 5 (d) -5
- (26) If  $\beta = 4 + 3x - 2x^2$  is a vector in the vector space  $P_2$ , then  $\|\beta\|$  is —  
 (a)  $\sqrt{7}$  (b)  $\sqrt{21}$  (c) 5 (d)  $\sqrt{29}$ .

(27) If  $\|u\| = \sqrt{18}$ ,  $\|v\| = \sqrt{12}$  and  $\langle u, v \rangle = -6$ , then  $\cos \theta$  is —

- (a)  $\frac{6}{\sqrt{18}\sqrt{12}}$  (b)  $\frac{1}{\sqrt{6}}$  (c)  $-\frac{1}{\sqrt{6}}$  (d) None.

(28) The values of  $k$  for which  $u = (k, -4, 8)$  and  $v = (k, k, -4)$  are orthogonal in Euclidean Inner Product Space  $\mathbb{R}^3$  are —

- (a) 4, -8 (b) -4, -8 (c) 8, -4 (d) 4, 8.

(29) The matrix  $A = \begin{bmatrix} \frac{3}{7} & \frac{2}{7} & \frac{6}{7} \\ -\frac{6}{7} & \frac{2}{7} & \frac{2}{7} \\ \frac{2}{7} & \frac{6}{7} & -\frac{3}{7} \end{bmatrix}$  is —

- (a) Hermitian (b) Orthogonal (c) Unitary (d) Skew-symmetric.

(30) If  $2x^2 + 6xy - 5y^2$  is the quadratic form, then associated symmetric matrix is —

- (a)  $\begin{bmatrix} 2 & -3 \\ -3 & -5 \end{bmatrix}$  (b)  $\begin{bmatrix} 2 & 3 \\ 3 & -5 \end{bmatrix}$  (c)  $\begin{bmatrix} 2 & 3 \\ 3 & 5 \end{bmatrix}$  (d)  $\begin{bmatrix} 2 & -3 \\ -3 & 5 \end{bmatrix}$

(31) If  $\begin{bmatrix} 6 & -6 \\ -6 & 3 \end{bmatrix}$  is the associated symmetric matrix, then quadratic form is —

- (a)  $6x^2 + 3y^2 + 12xy$  (b)  $6x^2 + 3y^2 - 12xy$  (c)  $6x^2 - 6y^2 + 3xy$  (d) None.

(32) The eigenvalues of Hermitian matrix are —

- (a) Complex only (b) Complex and real both (c) always real (d) always zero.

(33) For which values of  $a$  &  $b$ , the matrix  $\begin{bmatrix} 1 & 1+i & 2+6i \\ a & 2 & 2-4i \\ 2-6i & b & 3 \end{bmatrix}$  is Hermitian?

- (a)  $a = 1+i$ ,  $b = 2-4i$  (b)  $a = 1+i$ ,  $b = 2+4i$  (c)  $a = 1-i$ ,  $b = 2+4i$  (d)  $a = 1-i$ ,  $b = 2-4i$ .

(34) If a square matrix 'A' is such that  $A^{-1} = A^*$ , then 'A' is —

- (a) Hermitian (b) Skew-Hermitian (c) Unitary (d) None.

(35) If  $T: V \rightarrow V$  is an operator such that  $T(u) = 1$ ,  $\forall u \in V$ , then

- (a)  $T$  is linear (b)  $T$  is not linear (c)  $T$  is isomorphism (d) None

(36) Let  $T: \mathbb{R}^5 \rightarrow \mathbb{R}^4$  is a linear transformation with rank 3, then no. of basis elements in the kernel of  $T$  is — (a) 1 (b) 2 (c) 3 (d) 4

(37) If  $T: M_{33} \rightarrow \mathbb{R}^8$  is a linear transformation with rank 6, then nullity of  $T$  is —

- (a) 2 (b) 3 (c) 4 (d) 15.

(38) Let  $T: \mathbb{R}^2 \rightarrow \mathbb{R}^2$  be a linear operator given by  $T(x_1, x_2) = (x_2 - x_1, -2x_1 + 2x_2)$ . Which of the following vector is in  $\ker(T)$  —

- (a)  $(-1, 1)$  (b)  $(1, -1)$  (c)  $(1, 1)$  (d)  $(-1, 2)$ .



39) Which of the following sets of eigenvalues have a dominant eigenvalue —  
 (a)  $\{-10, 0, 1, 10\}$  (b)  $\{5, -5, 3, 2\}$  (c)  $\{-4, -3, 0, 1\}$  (d) None.

40) The singular values of the matrix,  $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \\ 1 & 0 \end{bmatrix}$  are —

(a) 1, 3 (b) 3, 2 (c) 1,  $\sqrt{3}$  (d) 3,  $\sqrt{3}$ .

41) If  $B = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$  be a matrix where  $B = A^T A$ , then singular values of A are —

(a) 1, 3 (b) 3, 2 (c) 1,  $\sqrt{3}$  (d) 3,  $\sqrt{3}$ .

42) In minimization problem, optimal solution occurring at corner point yields —

(a) mean value of objective function (b) mid-value of objective function  
 (c) lowest value of objective function (d) highest value of objective function.

43) The valid objective function for a LPP is —

(a)  $\max(x_1, x_2)$  (b)  $\min(x_1^2 + x_2^2)$  (c)  $\min(x_1 + x_2 - \frac{1}{3}x_3)$  (d)  $\min\left\{\frac{x_1}{x_3} + \frac{x_2}{x_3}\right\}$ .

44) Which of the following constraints is not linear?

(a)  $7x - 6y \leq 45$  (b)  $x + y + 3z \geq 35$  (c)  $2xy + x = 15$  (d)  $x + \frac{1}{2}y = 10$ .

45) The point (3, 2) satisfy one of the following systems —

(a)  $2x + 3y \geq 11$   
 $2x - 3y \geq 0$  (b)  $2x + 3y = 12$   
 $2x - 3y \geq 0$  (c) both (a) & (b) (d) Neither (a) nor (b).

### ANSWERS

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|-----|-----|-----|-----|-----|
| ① c | ⑪ c | ⑳ c | ⑳ b | ㉑ c |
| ② a | ⑫ c | ㉑ b | ㉑ c | ㉒ c |
| ③ b | ⑬ b | ㉒ b | ㉒ c | ㉓ c |
| ④ a | ⑭ b | ㉒ c | ㉓ c | ㉔ c |
| ⑤ d | ⑮ b | ㉓ c | ㉓ b | ㉕ b |
| ⑥ c | ⑯ d | ㉔ d | ㉔ b |     |
| ⑦ b | ⑰ b | ㉔ c | ㉕ b |     |
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